

## **LESSON 6**

- LEVEL INDICATORS
  - Superscripts
  - Baseline Indicator
  - Subscripts
  - More about Superscripts and Subscripts

### *Format*

- Itemized Material with Subdivisions
- Tabular Format
- Margins for Exercise Sets

### *Answers to Practice Material*

## **LESSON PREVIEW**

This lesson begins by looking at format. Itemized material with subdivisions is found throughout math textbooks, in exercise sets, and in answer sections. The rules differ somewhat from those followed in a nontechnical transcription. The topic of superscripts and subscripts is presented. Superscript, subscript, and baseline indicators are introduced. The lesson ends with another look at grouping signs as they relate to level indicators.





*Example 6-4*

5. Does the method of creating whole number x-terms work with decimals? Consider this example.

A jacket is marked 15% off. The sale cost is \$36.31. Expressed as an equation,  $0.85x = 36.21$ .

- a. What is the meaning of 0.85 in the equation?
- b. To eliminate the decimal, multiply both sides of the equation by a number that will result in an integer coefficient.

Can you find such a number? If you can, list at least one. If you cannot, explain why not.

c. Now solve the equation. What was the original price of the jacket?

6. ...

Braille representation of the text above, showing indentation and paragraph structure.

*In Nemeth, indentation of the first line of each new paragraph organizes the narrative. A blank line precedes and follows the displayed word problem, as directed by Braille Formats guidelines for displayed material, but the blocked*



**PRACTICE 6A**

23. Simplify and solve each equation below for  $x$ . Show your work and check your answer.

a.  $24 = 3x + 3$       b.  $2(x - 6) = x - 14$

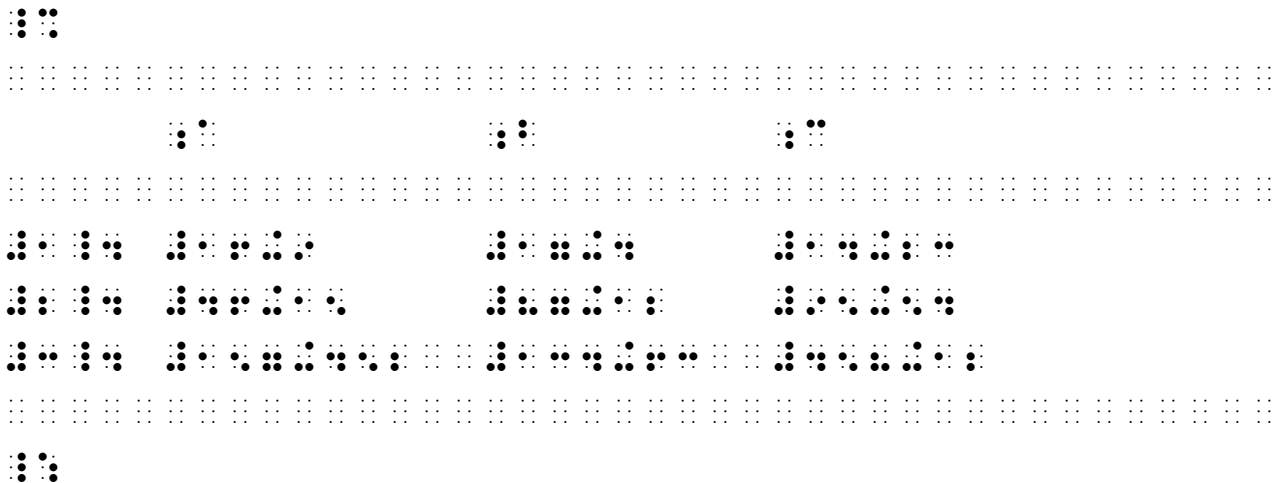
c.  $6 + 2.5x = 21$       d.  $2(x + 4.5) = 32$

6.1.3 **Tabular Format.** When itemized material is arranged in tabular form so that items are numbered at the margin and subdivisions are aligned beneath lettered column headings, the material should be transcribed in one of the following ways, depending upon whether all of the columns can be accommodated across the braille page.

a. **When to Retain Column Format.** If all the columns can be accommodated across the braille page, the print columnar arrangement is followed. Each problem number begins in cell 1. The letter identifying each column is aligned with the first cell of the related column. A blank line is left above and below the lettered column headings. Two blank cells separate the columns. Guide dots are not used.

Example 6-7

	a	b	c
1.	16 + 9	17 + 4	14 + 23
2.	46 + 15	87 + 12	95 + 54
3.	157 + 452	134 + 63	458 + 12



b. **When Not To Retain Column Format.** If all the columns cannot be accommodated across the braille page, each subdivision in each problem must be lettered individually and the format in Section 6.1 must be followed.

*Example 6-8*

	a	b	c	d
1.	16 + 9	17 + 4	14 + 23	37 + 18
2.	46 + 15	87 + 12	95 + 54	101 + 43
3.	157 + 452	134 + 63	458 + 12	935 + 298

⠠⠠

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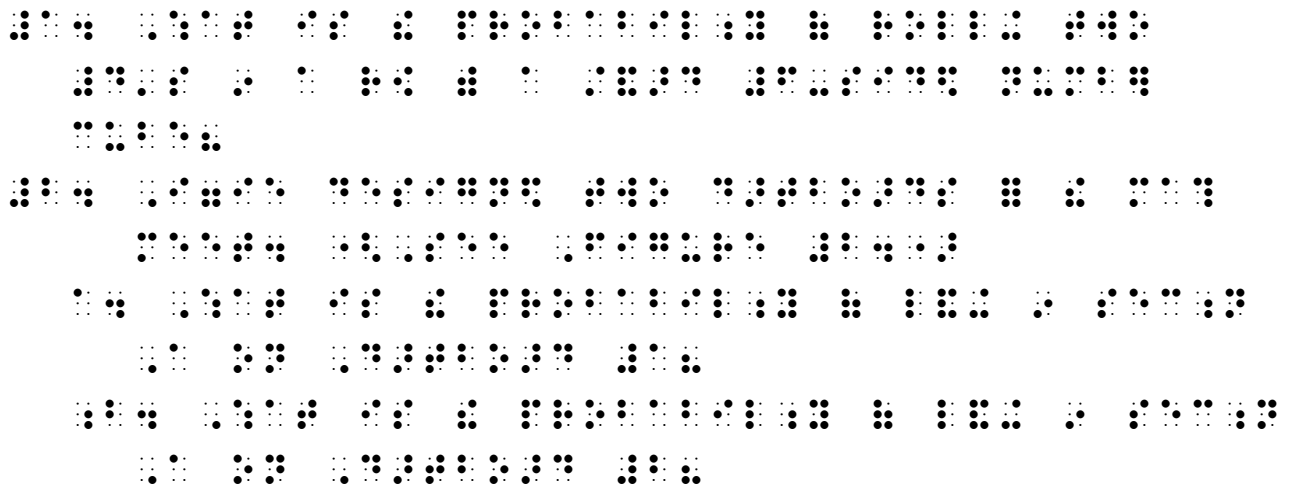
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⠠⠠ ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

6.1.4 **Varied Margins.** Runover margins for itemized material are determined individually for each item. That is, an item with no subdivisions will be (1-3); the next item may have subdivisions and so will be (1-5; 3-5), etc.

*Example 6-9*

1. What is the probability of rolling two 4's in a row with a standard 6-sided number cube?
2. Iggie designed two dartboards for the math meet. (See Figure 2.)
  - a. What is the probability of landing in section A on Dartboard 1?
  - b. What is the probability of landing in section A on Dartboard 2?











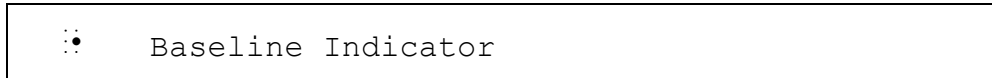


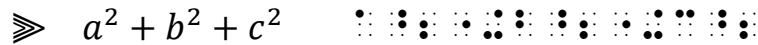


## *Introduction to the Baseline Indicator*

### 6.6 Function of the Baseline Indicator

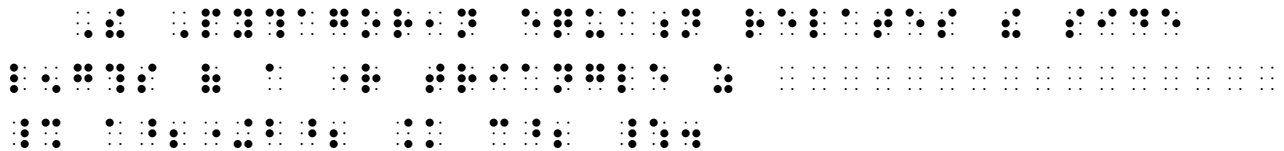
In an unspaced expression, a return to the baseline level is brought about by the use of the baseline indicator. Notice that the baseline indicator is the same symbol as the multipurpose indicator—dot 5. The indicator's function is understood in context.





#### Example 6-21

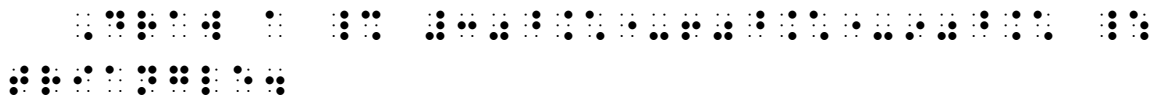
The Pythagorean equation relates the side lengths of a right triangle as  $a^2 + b^2 = c^2$ .



*The baseline is re-established before the plus sign.*

#### Example 6-22

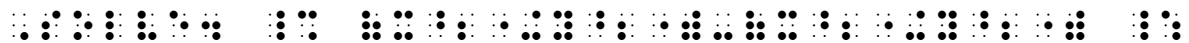
Draw a 30°-60°-90° triangle.



*The baseline is re-established before each hyphen.*

#### Example 6-23

Solve.  $(x^2 + y^2) - (x^2 + y^2)$



*The baseline is re-established before each plus sign and before each right parenthesis.*

**6.6.1 Degrees Fahrenheit and Degrees Celsius.** The abbreviations F (Fahrenheit) and C (Celsius) are given special consideration. Follow print spacing when these abbreviations are printed with a degree sign (raised hollow dot). A baseline indicator will be required when the degree sign is unspaced from the letter. Note that, when the letter stands alone, an English-letter indicator is required, but when the letter is unspaced from the raised hollow dot, an English-letter indicator is no longer needed. F and C are punctuated in literary mode when spaced away from the degree

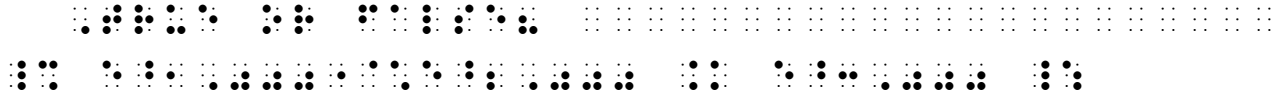






Example 6-27

True or false?  $e^{1,000} \times e^{2,000} = e^{3,000}$



*When a space brings the reader back to the baseline, a baseline indicator is not needed.*

**6.8 Certain Raised Signs**

Some signs are printed in a raised position but are not considered to be superscripts.

6.8.1 **Raised Ordinal.** *Braille Formats* states that raised ordinal endings are not considered to be superscript. This guideline is also followed in a technical transcription.

Example 6-28

Name the 3<sup>rd</sup> and 4<sup>th</sup> item in the series.



*The ordinal endings are printed in the raised position.*

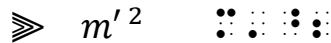
Example 6-29

What is the 3n<sup>th</sup> degree?

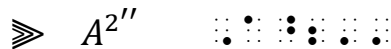


*"th" is printed in the raised position.*

6.8.2 **Prime Sign.** The prime sign appears to be raised in print but it assumes the same level as the number or letter to which it applies.



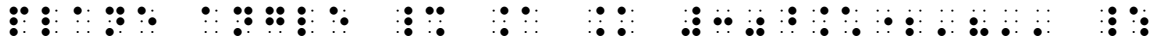
*The prime sign belongs with the letter m. Only the number 2 is in the superscript position.*



*The prime signs belong with the number 2 in the superscript.*

Example 6-30

plane angle  $\alpha = 30^\circ 2' 8''$



*The prime signs are not superscripts. They apply to numbers at the baseline of writing.*

6.8.3 **Apostrophe-s.** In an apostrophe-s ending, the apostrophe is at the same level as the "s". Because a punctuation indicator returns the reader to the baseline, a level indicator is inserted to maintain the level of the apostrophe-s.



*The apostrophe-s applies to  $m+m+m$ .*

Compare to this example where the "s" and its apostrophe are printed on the baseline level.



*The apostrophe-s applies to the entire expression  $A^{m+m+m}$ .*

**PRACTICE 6E**

1. Use a calculator to find  $9^{9^9}$ .
2. Find the  $r^{\text{th}}$  term of  $(x + y)^n$ .
3. Label the  $x^2$ 's and  $x^3$ 's.
4. What is the meaning of  $x''^3$ ?
5. Simplify:  $(x^3 - y^3)^2 - (x^3 + y^3)^2$ .
6.  $x^{y^nz}$  or  $x^{y^2z}$

## *Subscripts*

### 6.9 Subscript Level Indicators

Except as stated in Section [6.11](#) below, the subscript level indicator is used to show that the symbols immediately following it appear on the first level below the baseline of writing. Note that the subscript indicator is the same symbol as the English-letter indicator—dots 56. The indicator's function is understood in context.

⠠ Subscript Indicator

➤  $f_n$       ⠠ ⠠ ⠠

➤  $a_{(k+1)}$       ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠

Subscripts may carry subscripts of their own. In such cases, the subscript level indicator is doubled, tripled, etc. to indicate subscripts on the second, third, or lower levels.

⠠⠠ Subscript with Subscript  
(two levels below the baseline)

⠠⠠⠠ Subscript with Subscript with Subscript  
(three levels below the baseline)

➤  $n_{x_y}$       ⠠ ⠠ ⠠ ⠠ ⠠ ⠠

➤  $P_{x+1y+1z+1}$       ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠ ⠠

*Note:* The -?- in the second column is in the subscript position. The subscript of the second item in the fourth column is "minus two".

#### PRACTICE 6F

$3_c$	$10_8$	$?_3$	$x_{2+k}$
$3_{\text{five}}$	$10_{?-}$	$\text{Ca}(\text{OH})_2$	$y_{-2}$
$y_{n_k}$	$P_{3n}$	$a_{m1}$	$a_{m_1}$







6.11.2 **Restrictions.** Just because a numeral is a right subscript to a letter does not mean that the special rule can be applied. The subscript level indicator must be used if any of the following conditions apply:

- (1) If the letter is functioning as a numeral in a nondecimal numeration system, a subscript indicator is required.

➤ TE<sub>12</sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

*The subscript 12 means base-12 numeration.*

- (2) If the letter is part of a word or abbreviation, a subscript indicator is required.

➤ five<sub>3</sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

- (3) If the subscript contains any symbol other than a numeral with its comma or decimal point, a subscript indicator is required.

➤ x<sub>2k</sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

➤ x<sub>2'</sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

➤ x<sub>-2</sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

- (4) If the subscript carries a superscript or subscript of its own, a subscript indicator is required.

➤ x<sub>2<sub>n</sub></sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

- (5) Numeric subscripts on the second or lower levels always require their appropriate subscript level indicators.

➤ P<sub>n<sub>1</sub></sub> ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

6.11.3 **Summary.** The rules regarding use/nonuse of the subscript indicator are summarized below.

- a. A subscript level indicator is not used before a numeric subscript on the first level below the baseline of writing when the numeral is a right subscript to a letter. Furthermore, the following may also be true.
  - The numeric subscript may contain a segmenting comma or a decimal point.
  - The baseline letter may carry one or more primes or a superscript.
  - The baseline letter may be from any alphabet.
  - The baseline "letter" may be a two-letter chemical element.

- b. A subscript level indicator must be used in the following circumstances.
- A numeral on the first level below the baseline requires a subscript indicator if the subscript contains any symbol other than a numeral with its comma or decimal point.
  - A numeral on the first level below the baseline requires a subscript indicator if the subscript carries a superscript or subscript of its own.
  - A subscript on the second or lower level always requires the appropriate subscript level indicator.
  - If the subscript is a letter that is part of a word or an abbreviation, a subscript indicator is required.
  - If the subscript is a letter functioning as a numeral in a nondecimal numeration system, a subscript indicator is required.

### PRACTICE 6H

- 1) These expressions need subscript indicators:  $y_{-2}$ ,  $x_{2+k}$ ,  $a_{m1}$ ,  $x_{3n}$ ,  $x_{y_2}$ .
- 2) These expressions do not need a subscript indicator:  $x_1$ ,  $ax_2$ ,  $\text{CO}_2$ ,  $z_{.4}$ ,  $\beta_2$ .
- 3) Decide whether these expressions require a subscript indicator and transcribe them correctly:  $\text{shape}_4$ ,  $Q'_{\ 2}$ ,  $\text{C}_6\text{Fe}_2\text{O}_{12}$ ,  $n_k$ ,  $x_{2k}$ ,  $P_{r_{st}}$ ,  $D_{56}$ ,  $G_{9,999}$ , and the hexadecimal number  $2\text{E}6\text{B}_{16}$ .
- 4) **Chemistry.** While  $\text{Na}_2\text{ZnCl}_4$  could be cooled in the normal way,  $\text{Na}_2[\text{CoCl}_4]$  had to be quenched in the liquid  $\text{N}_2$ .
- 5)  $f_1(x) = g(x) \cdot q_2(x) + f_2(x)$

## 6.12 Spaces Within Superscripts and Subscripts

A space usually returns the reader to the baseline. Various strategies are used to retain the level in effect when a space occurs within a superscript or a subscript.

6.12.1 **Commas.** *Review:* A comma followed by a space re-establishes the baseline. The return to the baseline starts at the comma. No baseline indicator is necessary.

$$\begin{array}{l} \gg x^2, y^2, z^2 \qquad \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \quad \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \quad \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \\ \gg (a_1, a_{1i}, a_{2i}) \qquad \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \quad \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \quad \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \ddot{\cdot} \end{array}$$





In the next example, the commas separate three terms at the subscript level, but each "n" has a subscript as well. The correct level of each comma is shown by shrewd use of level indicators.

$$\gg P_{n_1, n_2, n_3}$$

6.12.2 **Words, Abbreviations, and Letters.** If a subscript or a superscript contains a space between words, abbreviations, or letters, the level must be restated after the space. The level indicator is unspaced from the following word, abbreviation, or letter.

$$\gg n_{\text{obtuse angles}}$$

*The subscript indicator before the word "angles" shows that the word is in the subscript position.*

$$\gg n_{\text{st. angles}}$$

*The abbreviation st. (for "straight") has a related period. No punctuation indicator is used with abbreviations.*

Note that an English letter will not need an English-letter indicator in such a case because it is no longer a "single letter" as defined by the Nemeth Code. (See Section 3.10.1 in Lesson 3.) Using "surface S" as an example, as a superscript it is transcribed  $\text{S}_{\text{surface}}$ . As a subscript it is transcribed  $\text{S}_{\text{surface}}$ .

6.12.3 **Comparison Signs.** The space before a comparison sign returns the reader to the baseline, as illustrated in the next example.

$$\gg a^2 = a \cdot a$$

*The superscript is 2. The equals sign is on the baseline.*

If the comparison sign is within a superscript or a subscript, the level is reinstated before the comparison sign. The indicator is unspaced from the comparison sign. The space after a comparison symbol preserves the level that is already in effect.

$$\gg S_u = a$$

*The subscript is u = a. The level in effect extends through the space following the comparison sign.*







## More about Superscripts and Subscripts

### 6.13 Superscript and Subscript Combinations

Combinations of subscripts to superscripts or of superscripts to subscripts require level indicators composed of two or more braille symbols. Keeping in mind that level indicators relate to the baseline, transcribing these expressions is an exercise in logical thinking.

#### 6.13.1 Superscripts with Subscripts

⠠⠠⠠ Superscript With Subscript

➤  $x^{n_1}$  ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

*"n, subscript one" is in the superscript position. "1" is a supersubscript.*

➤  $2^{Y_0} = Y_1$  ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

*"Y, subscript zero" is in the superscript position. "0" is a supersubscript.*

*Reminder:* The subscript indicator is omitted for a numeric subscript to a letter only for subscripts that are located on the first level below the baseline of writing. The super/subscript indicator is needed to show a numeric subscript in the superscript position.

#### 6.13.2 Subscripts with Superscripts

⠠⠠⠠ Subscript With Superscript

➤  $x_n^2$  ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

*"n, superscript two" is in the subscript position. "2" is a subsuperscript.*

➤  $P_3^n$  ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

*"3, superscript n" is in the subscript position. "n" is a subsuperscript.*

*Reminder:* The subscript indicator is required when a numeric subscript to a letter carries a superscript or subscript of its own.





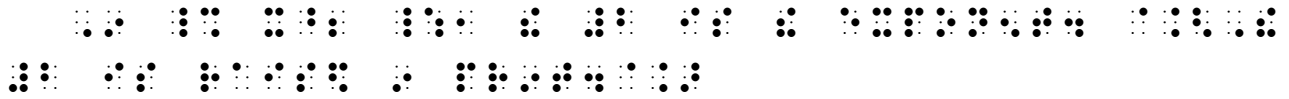






Example 6-43

In  $x^2$ , the <sup>2</sup> is the exponent.

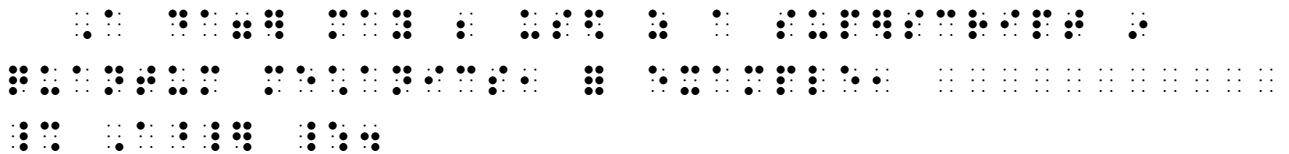


**6.20 Literary Symbols and Level Indicators**

If an ampersand, asterisk, crosshatch, dagger, double dagger, paragraph mark, or section mark is used mathematically and appears in a superscript or a subscript, its level must be indicated. The Nemeth symbols for these literary characters are listed in Lesson 5.

Example 6-44

A dagger may be used as a superscript in quantum mechanics, for example,  $A^\dagger$ .



**Summary**

Here is a summary of the difference in print among four types of superscripts and subscripts as defined in the Nemeth Code.

**Consecutive** A right super/subscript belongs to the preceding character and a left super/subscript belongs to the next character.

**Simultaneous** A character has both a superscript and a subscript. The superscript is printed directly above the subscript.

**Nonsimultaneous** A character has both a superscript and a subscript. The two scripts are not printed directly above and below each other.

**Detached** A super/subscript stands alone without being associated with a letter or number. It is printed slightly above or below the baseline and is smaller than the rest of the text.

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*Note:* There is no space between the subscript and the superscript in item #3.

### PRACTICE 6K

1. Here are some expressions with left superscripts:  ${}^3x$ ,  ${}^nx$ ,  
 ${}^{-2} + {}^{-4} = {}^{-6}$ ,  $(-3)^{-2+{}^{+2}}$ .
  2.  ${}^{12}_6\text{C}$  and  ${}^{12}\text{C}$  represent the same carbon isotope.
  3.  $\text{D}_2{}^{18}\text{O}$  is the doubly labeled water isotopologue!
  4. In  $\text{CO}_2$ , the subscript  ${}_2$  means "two oxygen atoms".
  5.  ${}_nP_r = K({}_{n-1}P_{r-1})$
  6.  $a_1^2 + b_1^2 + c_1^2$
  7.  $[t]_0^4$
  8.  $2 \times 10_6^2 + 3 \times 10_6^1 + 2$
  9.  $P_{xy}Q$
  10.  $\text{NH}_4^+ + \text{Cl}^- + \text{H}_2\text{O}$
-







PRACTICE 6C

- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9
- 10
- 11
- 12
- 13
- 14
- 15

*Runover margins for itemized material are determined individually for each question. Item 2 has subdivisions—its runover position (line 5) is cell 5.*





PRACTICE 6F

1     ⠠⠠

2     ⠠⠠⠠⠠     ⠠⠠⠠⠠⠠     ⠠⠠⠠     ⠠⠠⠠⠠⠠⠠

3     ⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠

4     ⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠

5     ⠠⠠

PRACTICE 6G

1     ⠠⠠⠠⠠     ⠠⠠⠠⠠     ⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠     ⠠⠠⠠⠠⠠⠠     ⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠     ⠠⠠⠠

2     ⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠

3     ⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠

4     ⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠

5     ⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠

6     ⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠     ⠠     ⠠⠠⠠     ⠠⠠⠠     ⠠⠠⠠

7     ⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

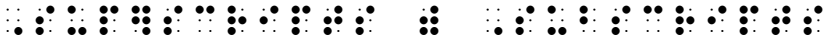
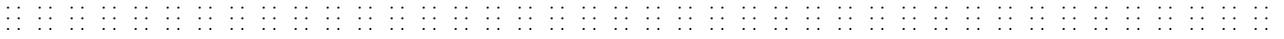





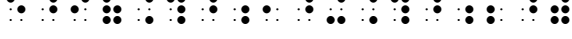

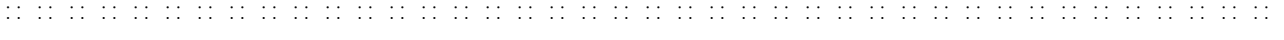

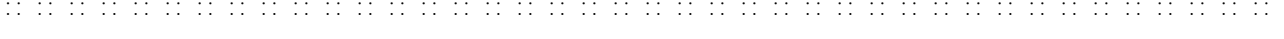


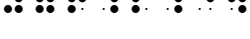
8     ⠠⠠⠠⠠⠠     ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠     ⠠⠠⠠



PRACTICE 6I

1.  $x_{1,2} \neq x^{i,j}$
2.  $x_{n-1,n-1}, x_{n-1,n}, x_{n,n-1}$
3.  $A^{n+n+n}$  all n's are equal.
4.  $s]_{t=a}$
5.  $e^{1,000}$
6.  $a^{m+k} \div a^m = a^k$
7.  $P_{s_1 \dots s_2}$  and  $P_{q_r, s}$
8.  $10_{-?-} = 6_8$
9.  $a'_1, a'_2, \dots, a'_n$  are the inverses.
10.  $\aleph_0$  represents the cardinality of the set of all natural numbers.

PRACTICE 6J

1. 
2. 
3. 
4. 
5. 
6. 
7. 
8. 
9. 
10. 
11. 
12. 
13. 
14. 
15. 
16. 