

## **LESSON 14**

- FUNCTION NAMES AND THEIR ABBREVIATED FORMS

*Spatial Arrangements, continued*

- SQUARE ROOT DIVISION
- OTHER PRINT LAYOUTS SHOWING DIVISION

*Answers to Practice Material*

### **LESSON PREVIEW**

Rules regarding function names and their abbreviated forms are presented. Many examples are shown. The study of spatial arrangements continues with other forms of division problems: square root division, partial quotient layout, synthetic division, and others.

## ***FUNCTION NAMES AND THEIR ABBREVIATED FORMS***

[NC Rule 18]

### **14.1 List of Common Function Names and Their Abbreviated Forms**

The most common function names and their abbreviated forms are listed below. Function names that do not appear in this list are subject to the same rules taught in this lesson. Note that abbreviated function names are printed in regular type.

<u>Function Name</u>	<u>Abbreviated Form</u>
amplitude	amp
antilogarithm	antilog
arc	arc
argument	arg
cologarithm	colog
cosine	cos
hyperbolic cosine	cosh
cotangent	cot
hyperbolic cotangent	coth
coversine	covers
cosecant	csc
hyperbolic cosecant	csch
cotangent	ctn
hyperbolic cotangent	ctnh
determinant	det
error function	erf
exponential	exp
exsecant	exsec
gradient	grad
haversine	hav
imaginary part	im
infimum	inf
limit	lim
upper limit	$\overline{\text{lim}}$ or $\overline{\text{limit}}$
lower limit	$\underline{\text{lim}}$ or $\underline{\text{limit}}$
natural logarithm	ln
logarithm	log
maximum	max
minimum	min
modulo	mod
real part	re
secant	sec







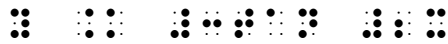




(2)  $\sin(\theta + 90^\circ) = \cos \theta$



(3)  $y = 3 \tan 2x$



(4)  $a^2 = 2ac \cos \beta + c^2$



(5)  $\sin(\alpha + \beta) + \sin(\alpha - \beta)$



(6)  $y' = x \cos \varphi - y \sin \varphi$



(7)  $2\sqrt{x} \sin \sqrt{x} + 2 \cos \sqrt{x} = C$



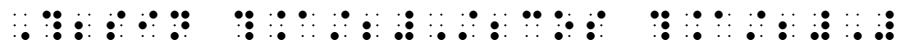
(8)  $6 \sin 2A \cos 4A$



(9)  $\cos 203^\circ \csc 203^\circ$



(10)  $\frac{2 \sin \frac{\alpha}{2}}{2 \cos \frac{\alpha}{2}}$



(11)  $\ln \left| \tan \left( \frac{\pi}{4} + \frac{x}{2} \right) \right| + C$



*"ln" is the abbreviated form of "natural logarithm". Refer to the table at the beginning of this lesson.*



---

**PRACTICE 14B**

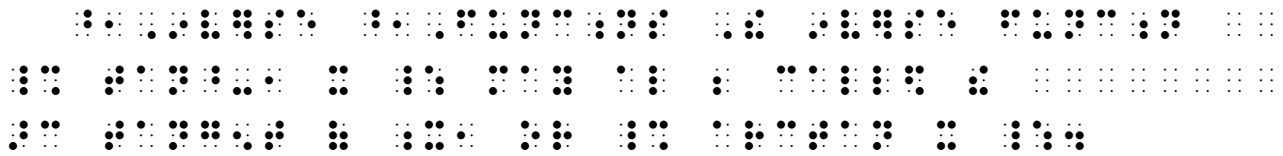
- (1)  $\sin \theta / \cos \theta$
  - (2)  $\sin 2\alpha = 2 \sin \alpha \cos \alpha$
  - (3)  $\frac{\tan 90^\circ}{\cot 90^\circ}$
  - (4)  $r[3 \cos \theta + 4 \sin \theta] = 5$
  - (5)  $7(\cos 20^\circ + i \sin 20^\circ)$
  - (6)  $\frac{1}{2} \ln |\sec 2t + \tan 2t| + C$
  - (7)  $a \sin \frac{x}{a} \cdot \frac{1}{a} = \sin \frac{x}{a}$
-





Example 14-16

**Inverse Functions** The inverse function  $\tan^{-1} x$  may also be called the arc tangent of  $x$ , or  $\arctan x$ .



*"arc tangent" is not divided between lines even though "arc" fits on the previous line.*

**14.6 Clarification—Function Names in an Enclosed List**

A function name and the item which follows it are regarded as a single item. Although the numeric indicator is not used at the beginning of an item in an enclosed list, it must be used before a numeral (or decimal point and a numeral) following a function name.

➤  $(2 \sin 30^\circ, 3 \cos 60^\circ)$



---

**PRACTICE 14C**

- (A)  $\sin x - \sin y$
  - (B)  $2 \sin x + 3 \cos y$
  - (C)  $\frac{1+\cos x}{\sin x} + \frac{\sin x}{1+\cos x}$
  - (D) The logarithm of  $\sin 18^\circ$  is written  $\log \sin 18^\circ$ .
  - (E)  $\cos 225^\circ = -\sqrt{\frac{1+\cos 450^\circ}{2}}$
  - (F)  $\text{ArcTan}[x, y]$  gives the arc tangent of  $\frac{y}{x}$ , taking into account in which quadrant the point  $(x, y)$  lies.
  - (G) The arc tangent of the complex number  $q$  is written " $\text{ArcTan}[q]$ ".
  - (H) Consider the ordered pair  $(\cos .8000, 2 \cos .8000)$ .
-





14.7.4 **Examples.** Study the following examples.

*Examples are in Nemeth. The code switch indicators are omitted from the simbraille.*

- (1)  $y = e^{\sin x}$       ⠠⠽ ⠠⠞⠢ ⠠⠑ ⠠⠎⠊⠎ ⠠⠭
- (2)  $y = e^{\text{sine } x}$       ⠠⠽ ⠠⠞⠢ ⠠⠑ ⠠⠎⠊⠎⠑ ⠠⠭
- (3)  $y = (\sin x)^{\tan x}$       ⠠⠽ ⠠⠞⠢ ⠠⠑ ⠠⠎⠊⠎ ⠠⠞⠠⠎ ⠠⠭
- (4)  $e^{\ln x - 2 \ln y}$       ⠠⠑ ⠠⠎⠊⠎ ⠠⠭ ⠠⠞⠠⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠭
- (5)  $a^{g(x) \log_a f(x)}$       ⠠⠁ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑
- (6)  $3^{\log_3 9}$       ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑

*Recall from Lesson 6 that a subscript indicator is required in superscript and subscript combinations. The super/sub indicator shows a numeric subscript in the superscript position.*

- (7)  $3^{\log_3 7} + 2^{\log_2 5}$   
 ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑

*Same note as (6), above.*

- (8)  $a^{\log_a x} = x$   
 ⠠⠁ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑

*Recall from Lesson 6 that the space before a comparison sign returns the reader to the baseline.*

- (9)  $e^{\sin x = a} > y$   
 ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑ ⠠⠎⠊⠎ ⠠⠑

*Recall from Lesson 6 that when a comparison sign occurs within a superscript, the level is restated before the comparison sign.*





## 14.8 Modifiers

Modified function names are transcribed according to the five-step rule for the transcription of modified expressions introduced in Lesson 12. When a function name carries a modifier, the required space after the function name follows the termination of the modifier.

$$\gg \lim_{x \rightarrow a}$$

$$\gg \lim_{x \rightarrow a} f(x) = 1$$



### 14.8.1 Examples. Study these additional examples.

*Examples are in Nemeth. The code switch indicators are omitted from the simbraille.*



$$(1) \lim_{x \uparrow 4} (x - 4)^{-1}$$



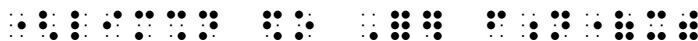
$$(2) \lim_{\theta \rightarrow \theta_0} (\tan \theta)$$



### 14.8.2 Special Case—Upper Limit and Lower Limit. The symbols below denote "upper limit" or "lower limit". The horizontal bar directly over or under "lim" or "limit" is not treated as a modifier.

	upper limit	$\overline{\text{lim}}$
	upper limit	$\overline{\text{limit}}$

$$\gg \overline{\lim}_{n \rightarrow \infty} f_n(x)$$



$$\gg \overline{\text{limit}}_{n \rightarrow \infty} f_n(x)$$



⠠⠠⠠⠠	lower limit	<u>lim</u>
⠠⠠⠠⠠⠠⠠	lower limit	<u>limit</u>

⦿  $\underline{\lim}_{n \rightarrow \infty} f_n(x)$

⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

⦿  $\underline{\text{limit}}_{n \rightarrow \infty} f_n(x)$

⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

**PRACTICE 14E**

1. Find  $\lim_{x \rightarrow 0.6} 2^{25x^2 - 10x - 1}$ .
2. Formulate a precise definition for  $\lim_{x \downarrow -\infty} f(x) = L$ .
3. If  $\overline{\lim}_{n \rightarrow \infty} a_n = A$  and  $\overline{\lim}_{n \rightarrow \infty} b_n = B$ , must it be true that  $\overline{\lim}_{n \rightarrow \infty} (a_n + b_n) = A + B$ ?
4. Find  $\overline{\lim}_{n \rightarrow \infty} a_n$  when  $a_n = (-1)_n$ .
5.  $\lim_{x \rightarrow 0} \csc x \ln(1 + x)$

# Spatial Arrangements, continued

You may wish to revisit the Review of Format for Spatial Arrangements in Lesson 10. NOTE: Code switch indicators are omitted and blank lines are implied in the examples that do not contain narrative.

## SQUARE ROOT DIVISION

[NC Rule 25.6]


### 14.9 Review of Terminology

Radical expressions were presented in Lesson 8. When an answer is shown, a spatial arrangement is required. Here are the names of the parts of a radical expression. The line above the radicand is the vinculum.  $\sqrt{\phantom{x}}$  is the radical sign.

$$\frac{12}{\sqrt{144}}$$
 root radicand

### 14.10 Spatial Arrangement for Square Root Problems

In the spatially arranged radical expression, the first cell of the vinculum is placed directly above the radical symbol. The last cell of the vinculum extends one cell beyond the radicand.

$\sqrt{\phantom{x}}$		
	Radical (with Vinculum)	$\sqrt{\phantom{x}}$

#### Example 14-20

The square root of 144 is 12, and is written as follows.

1	$12$
2	$\sqrt{144}$
3	 
4	 
5	 
6	 
7	 
8	 

*Lines 5-6: The leftmost braille cell of the displayed spatial expression is in cell 3 (displayed to 3-1 narrative).*

- a. **Solving a Square Root Problem.** The procedures used with long division arrangements are applied to a spatially arranged square root problem. Review alignment and spacing rules for long division in Lesson 10 and adapt the layout and alignment to resemble the print arrangement as closely as possible. The vinculum is transcribed as a separation line. The vertical line that separates the parts of the problem is represented by dots 456. Follow print regarding the column in which the vertical line is placed. This may mean placing it in the same column as a digit. (See [Example 14-22](#).)

Example 14-21 |

1	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		6. 4 8
2	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		√42.00 00
3	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		36
4	⠠⠠⠠⠠		124   600
5	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		× 4 496
6	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		1288   104 00
7	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		× 8 103 04
8	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		96
9	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		
10	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		
11	⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠		
12	⠠⠠⠠⠠		

All lines: Spacing between digits matches print in order to attain proper vertical alignment.  
 Line 2: The vinculum begins in the cell above the radical symbol and ends one cell beyond the rightmost character in the entire arrangement.  
 Lines 2, 5, 8, 11: Separation lines are all the same width.  
 Lines 6, 7, 9, 10: The vertical line in this problem aligns below the radical symbol, as printed. It is unspaced from the number to its left.  
 Lines 7, 10: The multiplication cross is unspaced from the multiplier.

Example 14-22

1	⠠⠠⠠	
2	⠠⠠⠠⠠⠠⠠⠠⠠	406
3	⠠⠠⠠⠠⠠⠠⠠	√164836
4	⠠⠠	16
5	⠠⠠⠠⠠⠠⠠⠠⠠	80   48
6	⠠⠠⠠ ⠠⠠	0   00
7	⠠⠠⠠ ⠠⠠	806   4836
8	⠠⠠⠠⠠⠠⠠⠠⠠	6   4836
9	⠠⠠⠠⠠⠠⠠⠠⠠ ⠠⠠⠠⠠	
10	⠠⠠ ⠠⠠⠠⠠	

*Lines 6-7: This vertical line is aligned beneath the radical symbol, as printed. It is unspaced from the number to its left.*

*Lines 9-10: This vertical line falls in the same column as some digits. It is unspaced from the number to its left.*

**14.11 Placement of Identifiers with Spatial Radical Expressions**

An identifier, if present, is placed on the line with the radicand. One blank space is left between the last symbol in the identifier and the symbol furthest left in the overall arrangement, including separation lines.

Example 14-23

	⠠⠠⠠	
	⠠⠠⠠⠠⠠⠠⠠⠠	4. 7 4.
	⠠⠠⠠⠠⠠⠠⠠	√5476.
	⠠⠠	49
	⠠⠠⠠⠠⠠⠠⠠⠠	144   576
	⠠⠠⠠ ⠠⠠	576
	⠠⠠⠠ ⠠⠠	
	⠠⠠⠠⠠⠠⠠⠠⠠	
	⠠⠠⠠⠠⠠⠠⠠⠠ ⠠⠠⠠⠠	
	⠠⠠ ⠠⠠⠠⠠	

---

PRACTICE 14F

(A)  $\sqrt{33.0000}$

$$\begin{array}{r} 5.74 \\ \hline 25 \\ \hline 107 \overline{) 800} \\ \times 7 \quad \underline{749} \\ 1144 \overline{) 5100} \\ \times 4 \quad \underline{4576} \\ 524 \end{array}$$

---

## OTHER PRINT LAYOUTS SHOWING DIVISION

In the next two layouts, note that the rules regarding placement of the vertical line differ from each other, and also differ from the vertical line rules in a square root problem ([14.10.a](#)). Before transcribing, analyze the print and refer to the appropriate rules.

### 14.12 Partial Quotients [NC Rule 25.5.8]

This layout shows partial quotients printed to the right of the division problem. A vertical line separates the partial quotients from the rest of the problem. The partial quotients may or may not be aligned by place value.

The vertical line may be either drawn as a tactile graphic or it may be represented by dots 456. The partial quotients are aligned as printed. Space is left between the vertical line and any digit preceding or following it. More than one space may be needed if the partial quotients are aligned by place value.

No space is inserted between a separation line and the vertical line.

Example 14-24

	<table style="border-collapse: collapse; margin: auto;"> <tr> <td style="border-right: 1px solid black; padding-right: 5px;">7</td> <td style="border-bottom: 1px solid black; padding: 0 5px;">539</td> <td style="border-left: 1px solid black; padding-left: 5px;"></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">70</td> <td style="border-left: 1px solid black; padding-left: 5px;">10</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">469</td> <td style="border-left: 1px solid black; padding-left: 5px;"></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">140</td> <td style="border-left: 1px solid black; padding-left: 5px;">20</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">329</td> <td style="border-left: 1px solid black; padding-left: 5px;"></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">210</td> <td style="border-left: 1px solid black; padding-left: 5px;">30</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">119</td> <td style="border-left: 1px solid black; padding-left: 5px;"></td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="border-bottom: 1px solid black; padding: 0 5px;">119</td> <td style="border-left: 1px solid black; padding-left: 5px;">17</td> </tr> <tr> <td style="border-right: 1px solid black; padding-right: 5px;"></td> <td style="padding: 0 5px;">77</td> <td style="border-left: 1px solid black; padding-left: 5px;"></td> </tr> </table>	7	539			70	10		469			140	20		329			210	30		119			119	17		77	
7	539																											
	70	10																										
	469																											
	140	20																										
	329																											
	210	30																										
	119																											
	119	17																										
	77																											

*Notice the comparative lengths of the separation lines as well as their vertical alignment.*

---

*Instructions:* Review Section 10.13.6.d regarding alignment of the minus signs.

**PRACTICE 14G**

$$\begin{array}{r|l} 132 & \\ 6 \overline{)792} & \\ \underline{-600} & 100 \\ 192 & \\ \underline{-60} & 10 \\ 132 & \\ \underline{-60} & 10 \\ 72 & \\ \underline{-60} & 10 \\ 12 & \\ \underline{-12} & 2 \\ 0 & \end{array}$$



### 14.13 Synthetic Division [NC Rule 25.7]

Synthetic division is a method of showing division of polynomials. There is not a standard print layout. The transcription replicates the print design, following alignment rules discussed below, and using the separation line and vertical line of the Nemeth Code. Here is an example of one possible layout of a synthetic division problem.

$$\begin{array}{r|rrrr}
 +2 & 1 & -3 & +4 & +5 \\
 & & +2 & -2 & +4 \\
 \hline
 & 1 & -1 & +2 & +9
 \end{array}$$

The parts to this problem are labeled as follows.

$$\begin{array}{r|rrrr}
 \textit{synthetic divisor} & +2 & 1 & -3 & +4 & +5 & \textit{synthetic dividend} \\
 & & & +2 & -2 & +4 & \textit{synthetic product} \\
 \hline
 \textit{synthetic quotient} & & 1 & -1 & +2 & +9 & \textit{synthetic remainder}
 \end{array}$$

14.13.1 **Alignment and Spacing.** In the examples which follow, look carefully at the vertical alignment. The numerals in the synthetic dividend, product, and quotient are aligned by place value. Symbols of operation are vertically aligned. (See [Example 14-29](#).) At least one column of blank cells comes between adjacent columns.

14.13.2 **Vertical Line and Separation Line.** Dots 456 represent the vertical line in the print copy. The line comes between the synthetic divisor and the division arrangement. It begins on the line with the dividend and ends on the line with the product. No space is left between the vertical line and the dividend or divisor. Another vertical line may appear between the synthetic quotient and the synthetic remainder. It is transcribed below a blank column.

The separation line (dots 25) begins directly under the vertical line at one end, and terminates one cell beyond the overall arrangement at the other end.

Example 14-25

$$\begin{array}{r|rrrr}
 +2 & 1 & -3 & +4 & +5 \\
 & & +2 & -2 & +4 \\
 \hline
 & 1 & -1 & +2 & +9
 \end{array}$$

$$\begin{array}{r|rrrr}
 +2 & 1 & -3 & +4 & +5 \\
 & & +2 & -2 & +4 \\
 \hline
 & 1 & -1 & +2 & +9
 \end{array}$$

Note the vertical alignment of the numerals and the operation symbols, the spacing of the vertical line, and the length of the separation line.

14.13.3 **Another Print Style—Synthetic Divisor on the Right.** If the synthetic divisor is printed to the right of the overall problem, the same layout is followed in braille. Follow the alignment and spacing rules outlined above, particularly noting that at least one blank cell must be left between adjacent columns. The vertical lines are unspaced from the dividend and the divisor, as well as from the quotient and the remainder.

Example 14-26 |

$$\begin{array}{r|rrrr} 3 & -7 & -1 & -23 & 3 \\ & +9 & +6 & +15 & \\ \hline 3 & +2 & +5 & & -8 \end{array}$$

14.13.4 **Another Print Style—Boxed Synthetic Divisor.** If the synthetic divisor appears boxed on two sides, the boxing is omitted. A vertical line between the divisor and the dividend is inserted in order to differentiate the divisor from the rest of the arrangement, even though this vertical line does not appear in print. Follow the same alignment and spacing rules outlined above. The first example shows the divisor at the left; the second example shows the synthetic divisor at the right.

Example 14-27 |

$$\begin{array}{r|rrrr} \boxed{-1} & 1 & +2 & +2 & +4 \\ & & -1 & -1 & -1 \\ \hline 1 & +1 & +1 & & +3 \end{array}$$

Example 14-28

$$\begin{array}{r}
 1 \quad +2 \quad +2 \quad +4 \quad | \quad -2 \\
 \quad -2 \quad +0 \quad -4 \\
 \hline
 1 \quad +0 \quad +2 \quad +0
 \end{array}$$

$$\begin{array}{r}
 \cdot \quad \cdot \cdot \cdot \quad \cdot \cdot \cdot \quad \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\
 \quad \cdot \cdot \cdot \quad \cdot \cdot \cdot \quad \cdot \cdot \cdot \cdot \\
 \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\
 \cdot \quad \cdot \cdot \cdot \quad \cdot \cdot \cdot \quad \cdot \cdot \cdot
 \end{array}$$

*Note that this example has no remainder.*

14.13.5 **Placement of Identifiers with Synthetic Division.** An identifier, if present, is placed on the line with the dividend (the top line of the arrangement, in this case). One blank space must be left between the last symbol in the identifier and the symbol furthest left in the overall arrangement, including separation lines.

Example 14-29

$$\begin{array}{r}
 197. \quad | \quad +2 \quad 1 \quad +6 \quad -1 \quad -30 \\
 \quad \quad \quad \quad \quad \quad \quad +2 \quad +16 \quad +30 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 \cdot \cdot \cdot \cdot \cdot \cdot \cdot \quad \cdot \cdot \cdot \cdot \cdot \cdot \quad \cdot \cdot \cdot \quad \cdot \cdot \quad \cdot \quad \cdot \cdot \cdot \cdot \cdot \\
 \quad \quad \quad \quad \quad \quad \quad \cdot \cdot \quad \cdot \cdot \cdot \cdot \quad \cdot \cdot \cdot \cdot \cdot \quad \cdot \cdot \cdot \cdot \cdot \\
 \quad \quad \quad \quad \quad \quad \quad \cdot
 \end{array}$$

*Notice the vertical alignment of the operation symbols with -1 and +16 even though they are not aligned in print.*

---

**PRACTICE 14H**

**Dividing Polynomials:** Divide  $(3x^4 + 12x^3 - 5x^2 - 18x + 8) \div (x + 4)$

$$\begin{array}{r|rrrrr} -4 & 3 & 12 & -5 & -18 & 8 \\ & & -12 & 0 & 20 & -8 \\ \hline & 3 & 0 & -5 & 2 & 0 \end{array}$$

*Answer:*  $3x^2 - 5x - 2$

---

*For further practice, see Appendix A—Reading Practice.*

**EXERCISE 14**

Prepare Exercise 14 for your grader.

# ANSWERS TO PRACTICE MATERIAL

## PRACTICE 14A

1     ⠠⠨⠠⠇   ⠠⠡⠠⠇   ⠠⠡⠠⠡⠠⠡   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠

2     ⠠⠠⠠⠠⠠⠠⠠

3     ⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠

4     ⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠

5     ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠

6     ⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠

7     ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠

## PRACTICE 14B

1     ⠠⠠⠠

2     ⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠

3     ⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠

4     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

5     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠

6     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

7     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠

8     ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠

PRACTICE 14C

1     ⠠⠠

2     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠   ⠠⠠⠠⠠⠠

3     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠   ⠠⠠⠠⠠⠠

4     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠

5     ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠

6         ⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠

7     ⠠⠠⠠⠠

8         ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠

9     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠

10         ⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠

11         ⠠   ⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠

12     ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠

13         ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠

14     ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠

15         ⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠

PRACTICE 14D

1     ⠠⠠

2     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠

3     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠

4     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠⠠⠠

5     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠

6     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠

7     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠

8     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠

9     ⠠⠠⠠⠠   ⠠⠠⠠⠠⠠⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠   ⠠⠠⠠



# PRACTICE 14F

1     ···

2     ..... (row of 18 dots)

3                 ··· ··· ···

4                 ·······

5     ··· ··· ···     ··· ··· ···     ··· ···

6                 ···

7                 ·····

8     ··· ··· ···     ···     ··· ···

9     ··· ··· ···     ···     ··· ···

10                ·····

11     ··· ··· ···     ···     ··· ···

12     ··· ··· ···     ···     ··· ···

13                ·····

14                         ··· ···

15     ..... (row of 18 dots)

16     ···





## PRACTICE 14H

1  
1  
2  
3  
4  
5  
6  
7  
8  
9

- Line 4: The leftmost braille cell of the displayed spatial expression is in cell 3 (displayed to 3-1 narrative).*
- Line 7: The remainder does not touch the vertical line because a space must be inserted in order to align with the numbers above the separation line.*