AN INTRODUCTION TO BRAILLE MATHEMATICS USING NEMETH CODE WITHIN UEB CONTEXTS A Course for Transcribers

Provisional Online Edition 2017

Revised by Lindy B. Walton Barbara Taffet, advisor

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I believe that I could not have reached my potential in mathematics without the Nemeth Code. With it, I am able to read and write mathematics, as well as other sciences, at all levels, limited only by my talent and my ambition. —Dr. Abraham Nemeth, creator of the braille code for

mathematics and science notation

DEDICATION

I credit my interest in the continued training of braille transcribers in the Nemeth Code to my friend and mentor, Helen Hay, whose fascination and enthusiasm about this braille code was contagious. —Lindy Walton

THANKS

I offer my gratitude to the original authors of this lesson manual, Helen Roberts, Bernard M. Krebs, and Barbara Taffet, for their insight into the learning process and for their eye for detail. Many of the excellent examples from the original book are preserved in this edition. I also wish to thank my supervisors and colleagues in the Madison Metropolitan School District for realizing the importance of the development of this curriculum. —Lindy Walton

ABOUT THE PROVISIONAL ONLINE EDITION

Due to the need to make this training manual available to transcribers as soon as possible, we are offering a provisional version of the lessons in downloadable electronic format before being completely field tested and while BANA is revising the Nemeth Code. Exercises at the end of each lesson will not be available until a path toward certification is established. You may proceed through the course as each lesson is released with the understanding that certain details are still under construction and that some rules may change. A certification exam will not be available until the revised Nemeth Code is released. To apply for the exam, you must have turned in passing transcriptions of each of the yet-to-be-released lesson exercises.

We encourage you to contact us to report errors or to comment on topics that are unclear. As a result of user feedback, you can expect changes to appear in the online edition. All changes will be documented. A running list will be maintained and will be posted on www.nfb.org/transcribers.

Once a final version is approved, this lesson book will also be available in printed form.

To contact us by e-mail, send your message to transcribers@nfb.org.

FOREWORD TO THE 2017 EDITION

The first edition of the *Introduction to Braille Mathematics* was published in 1978 and was written by the late Helen Roberts and Bernard M. Krebs. It was my privilege to complete the text with Mr. Krebs after Helen passed away. Since that time, numerous corrections and updates have been made both to the Nemeth Code itself and to this manual. Now, however, a major change has necessitated a complete re-writing of the lessons. 2016 was the implementation year in the United States for new transcriptions to be produced using the Unified English Braille Code. Because Nemeth Code works *within* UEB, many of the rules of Nemeth Code must be modified.

After the first lesson most examples, practices, and exercises are shown in a text-like context. In this way, the student can see how the Nemeth Code works in a real setting such as found in texts of many grade levels and complexities.

The practices within each lesson are available for self-checking by the student. Answers to the practices are given at the end of each lesson. Braille reading practice will soon be offered in Appendix A. In the future, each lesson will conclude with an exercise which will be graded and evaluated by your teacher or by your NFB-assigned grader.

The braille examples are written on a 38-cell line in the lesson manual to allow for a reasonable margin on the given page size. However, the student should use the standard 40-cell line when transcribing the practices and exercises.

The student should understand that the Nemeth Code itself is the authoritative source for all mathematics transcriptions. The student should also be thoroughly familiar with the sourcebooks listed in the PREREQUISITES which follow this Foreword.

It has long been my hope that this manual could be brought into the present era. Lindy Walton, an experienced transcriber who works with the NLS Nemeth certification program, led the writing of this Second Edition. Once again, it is my honor to work with an exceptional member of the braille transcriber community.

Both Lindy and I thank the following for their support and help: Mary Denault, Peggy Jackson, Bill Jackson, Kyle DeJute, Julie Sumwalt, Lynnette Taylor, the members of the BANA Nemeth Code Technical Committee, and the Grafton Braille Service Center. We would also like to thank the National Federation of the Blind which has lent support to the development and publication of this comprehensive manual.

Barbara Taffet

PREREQUISITES

A prerequisite to the study of the Nemeth Code within UEB context is certification in Unified English Braille, adequate experience in literary braille transcription, and confidence in your production method. Before beginning this course of study the student should also be thoroughly familiar with current methods for transcribing a textbook. Rules and guidelines are found in the following sourcebooks, all of which are from the Braille Authority of North available America (BANA) at www.brailleauthority.org. Dates shown below are the editions used as a resource in this lesson manual.

The Rules of Unified English Braille, Second Edition 2013 Guidance for Transcription Using the Nemeth Code within UEB Contexts, 2016 Braille Formats: Principles of Print-to-Braille Transcription, 2016 The Nemeth Braille Code for Mathematics and Science Notation, 1972 Revision, 2007–2015 Updates Guidelines and Standards for Tactile Graphics, 2010 Braille Code for Chemical Notation 1997

STUDY TIPS

HOW TO BECOME AN EXCELLENT NEMETH BRAILLE TRANSCRIBER

Don't race through the lesson material.

- Read carefully and deliberately as the narrative is compact and the language is exact.
- Study the examples and understand the point being made with each one but do not rely
 on the examples alone for an understanding of the rules. Braille the examples to
 reinforce the rule.
- Do the practice drills. Proofread them before checking the answers. See more tips below.
- Try back-translating the braille examples and practices without looking at the print.
- Take special note of rules regarding spacing, punctuation, abbreviations, and format.
- Make lists to help you remember differences between Nemeth and UEB rules.
- Don't be afraid to underline, highlight, or write notes in the margins of your lesson manual.

If the braille or the print doesn't make sense to you ...

- Compare new information to similar topics learned in previous lessons.
- Some of the lesson material is grouped in "use of" and "nonuse of." Compare them and look closely at the braille examples.

THE PRACTICE MATERIAL

- Slow down. By using 6-key entry instead of a translator you will better understand the braille from the reader's point of view.
- Compare your braille to the answers to the practice material found at the end of each lesson. Read each cell closely.
- At the end of each line, look at the braille cell in the line above and in the line below and compare it to the answer key. Any misalignment indicates an error on that line.
- When you identify your errors, return to the lesson to review the applicable rule.

PREPARING THE EXERCISE FOR GRADING

- Don't try to copy braille examples that look like the exercise material understand and apply the rule.
- Don't guess. Don't rely on the proofreader's report to find your mistakes.
- Proofread carefully before turning in for grading. Your knowledge and understanding of the Nemeth Code will improve dramatically if you proofread from an embossed copy or from a simulated braille (print) copy, without looking at the print.
- Make note of items you are unsure of. If your transcription is correct, look these items over again after receiving your report to reinforce the rule.

RESEARCH/REVIEW

- Analyze the mistakes found in your exercise and make sure you understand your errors before moving ahead to the next lesson. Ask questions until you are sure of the rule.
- Return to earlier lessons. Topics will make more sense to you in retrospect.
- Read the index. Terminology used there will help you understand the language of Nemeth braille.
- Review format rules learned in earlier lessons. Study the examples.
- Go back to an earlier lesson exercise and back-translate the practices or your braille exercise by writing in longhand. Don't look at the print copy until you are finished. Giving yourself some distance from the lesson material is a good review strategy.
- In later lessons, research the topic in the Nemeth Code in addition to studying the lesson book. Not only will this enrich your understanding of the current subject, you will also review material already learned in a new context.

PROOFREADING TIPS

Accuracy is crucially important in technical work. Your proofreading skills will be challenged.

- Is your lighting adequate?
- Use a magnifier when print is questionable.
- Use a straightedge when levels are in question.
- Take breaks when your concentration wanes. Then go back a few pages when resuming proofreading.
- Read the braille dots. Compare often to the print copy.
- Vary your reading medium -- don't always proofread from the screen or from simulated braille or from embossed braille.

BRAILLE TRANSLATION SOFTWARE

Many students of the Nemeth Code have been brailling for years and have thousands of pages of braille to their credit. They also have been taking advantage of the many electronic input and proofreading aids available to transcribers and are quite adept at turning out high quality work. We expect you are one of those transcribers.

You are undertaking a serious study of one of the technical braille codes, and we would like you to consider stepping back a bit and learning the old fashioned way, using 6-key entry in your braille software program. It is our experience that the best braille transcribers are those that can read and write braille as the 6-dot code that it is, not solely reading a back translation or a source file and not using another input code to 'type' math problems. Using proofreading and production aids for more accurate and faster work is certainly something you will continue to use – it is important that you understand how your particular software and translation tools work in Nemeth mode – but we are convinced you will understand the Code better if you take the 6-key approach while learning.

Best of luck to you!

CONTENTS

About the Provisional Online Edition Foreword to the 2017 Edition Prerequisites Study Tips

Lesson 1

1.1	Philosophy	
1.2	Non-technical and Technical Texts	
	1.2.1 Non-technical Texts	
	1.2.2 Technical Texts	
INTRODU	JCTION TO NUMERALS AND THE NUMERIC INDICATOR	
1.3	Representation of Arabic Numerals	
	1.3.1 English Braille Numerals	
	1.3.2 Nemeth Code Digits	
1.4	Numeric Indicator	
	1.4.1 Special Case: Segmented Numbers	
THE PRA	CTICE MATERIAL	Practice 1A
THE MAT	THEMATICAL COMMA AND DECIMAL POINT	
1.5	Mathematical Comma	
1.6	Mathematical Decimal Point	
	1.6.1 Spacing of the Decimal Point	
	1.6.2 The Decimal Point and the Numeric Indicator	
1.7	Format: General Principles	Practice 1B
INTRODU	JCTION TO SIGNS OF OPERATION	
1.8	Signs of Operation	
	1.8.1 Spacing with Signs of Operation	
	1.8.2 Positive and Negative Numbers	Practice 1C
INTRODU	JCTION TO SIGNS OF COMPARISON	
1.9	Signs of Comparison	
	1.9.1 Spacing with Signs of Comparison	Practice 1D
MONETA	RY, PERCENT, AND PRIME SIGNS	
1.10	Monetary Signs	
	1.10.1 Spacing with Monetary Signs	
1.11	Percent and Per Mille Signs	
	1.11.1 Spacing with Percent and Per Mille Signs	
1.12	Prime Sign	Practice 1E
CONTINE	ENTAL SYMBOLS	
1.13	The Continental Comma	
1.14	The Continental Decimal Point	

Answers to Practice Material

Lesson 2

INTRODUCTION TO CODE SWITCHING	
2.1 A Complete Transcription	
2.2 Use of the Switch Indicators	Practice 2A
2.3 Which Code?	
2.4 Placement of Literary Punctuation	Practice 2B
2.5 Format: Keep Together-General Principle Regarding Mathematical	
Expressions	
Placement of the Switch Indicators	
2.5.1 Keep Together If Possible	
2.5.2 A Switch Indicator May Stand Alone on a Line if	
Unavoidable	
2.5.3 Switch Indicators at Page Turns	Practice 2C
2.6 Consistency with Mathematical Symbols	Practice 2D
THE HYPHEN AND THE DASH	
2.7 The Hyphen and the Dash As Punctuation	
2.7.1 A Hyphen May Divide a Long Numeral	
2.7.2 A Hyphen May Connect Numerals	
2.7.3 A Dash Separates	
2.7.4 Hyphen, Dash, or Minus Sign?	Practice 2E
SIGNS OF OMISSION	
2.8 General Use of Signs of Omission	
2.9 Ellipsis	
2.10 Long Dash	
2.11 General Omission Symbol	
2.12 Other Omission Symbols	
2.13 Spacing of the Ellipsis and Long Dash	
2.14 : Paragraph Margins for Narrative Portions of Text (3-1)	Practice 2F
INTRODUCTION TO IDENTIFIERS	
2.15 Terminology	
2.16 Format: Margins for Itemized Material with No Subdivisions (1-3)	Practice 2G
FORMAT SUMMARY #1	
Answers to Practice Material	
Lesson 3	

MORE ABOUT PUNCTUATION 3.1 Punctuation Mode 3.2 Spacing of UEB Punctuation and Code Switch Indicators 3.2.1 Spacing of the UEB Dash 3.3 Nemeth Braille Punctuation

PUNCTUATION IN NEMETH CODE

- 3.4 Background
- The Punctuation Indicator
 - 3.5 Role of the Punctuation Indicator
 - 3.5.1 Comparison Sign in Quotes
 - 3.5.2 Number in Quotes
 - 3.5.3 Clock Time
 - 3.6 Punctuation with Omission Signs

3.6.1 SPACING EXCEPTION — The Hyphen

- 3.7 Punctuation and Spacing of Plural or Possessive Endings Practice 3B
- 3.8 SUMMARY—Situations That Do Not Require a Puncuation Indicator

INTRODUCTION TO SIGNS OF GROUPING

- 3.9 Definition
- 3.10 Signs of Grouping with Numerals
- 3.11 Punctuation with Grouping Symbols
- 3.12 Nested Grouping Symbols

Code-Switching Considerations

- 3.13 "Enclosed" Technical Material
 - 3.13.1 Punctuation Following a Sign of Grouping
- 3.14 The Bigger Picture

Spacing with Signs of Grouping

- 3.15 Spacing Inside of the Grouping Signs
- 3.16 Spacing Outside of the Grouping Signs

IDENTIFIERS, cont.

- 3.17 Code Switching and Identifiers—Maintaining Alignment
- 3.18 Context Decisions and Code Switching
- 3.19 Format: Keep Together—Hyphenated Expressions
- 3.20 *Format:* Margins for Itemized Material with No Subdivisions—Side-by-Side Layout

Answers to Practice Material

Lesson 4

WORDS

- 4.1 Words in Mathematical Context
 - 4.1.1 Capitalization
- 4.2 Words in Narrative
- 4.3 Punctuation With Words

Introduction to Abbreviations

- 4.4 Abbreviations
 - 4.4.1 *Format:* Keep Together

Practice 4A

Practice 3C

Practice 3D

	4.4.2 Punctuation with Abbreviations	
	4.4.2.a Abbreviations with a Related Period	
	4.4.3 Spacing with Abbreviations	
4.5	Numbers with Ordinal Endings	Practice 4B
Single-W	ord Switch Indicator	
4.6	The Single-Word Switch Indicator	
	4.6.1 Consider the Context	
	4.6.2 Lower Wordsigns	
	4.6.3 Two or More Words	
	4.6.4 Switch Considerations	
Switch In	ndicators at Page Turns, cont.	
4.7	Review of "Keep Together" Considerations	Practice 4C
4.8	New Print Page	
LETTERS		
4.9	Single English Letters in Narrative	
4.10	Single English Letters in Nemeth Code	
	4.10.1 Nemeth Code Definition of "Single Letter"	
Introduct	tion to the English Letter Indicator	
4.11	Use of the English Letter Indicator with a "Single Letter"	
	4.11.1 Capitalization of "Single Letters"	
	4.11.2 Punctuation of "Single Letters"	
	4.11.3 Mapping Notation	Practice 4D
4.12	Nonuse of the English Letter Indicator with a "Single Letter"	
	4.12.1 Comparison Sign	
	4.12.2 Enclosed Within Grouping Symbols	
	4.12.3 Unspaced Sequence of Terms	
	4.12.3.a Probability Notation	
4.13	Letters as Identifiers	Practice 4E
Mathema	itical Letter Combinations	
4.14	Mathematical Letter Sequence	
4.15	Capitalized Letter Sequence	
4.16	Shortform Letter Combinations	
	4.16.1 Use of the English Letter Indicator with a "Shortform Letter Combina	ation"
	4.16.2 Nonuse of the English Letter Indicator with a	
	"Shortform Letter Combination"	Practice 4F
FORMAT	SUMMARY #2	

Answers to Practice Material

Variable	S	
5.1	Mathematical Variables	
	5.1.1 Format: Keep Together	
	5.1.2 Abbreviation or Variable?	Practice
Roman N	Numerals	
5.2	Letter or Numeral?	
5.3	Transcribing Roman Numerals in Mathematical Context	
	5.3.1 Roman Numerals Consisting of Lowercase Letters	
	5.3.2 Roman Numerals Consisting of One Capital Letter	
	5.3.3 Roman Numerals Consisting of Two or More Capital Letters	
	5.3.4 Punctuation with Roman Numerals	
	5.3.5 Nonuse of the English Letter Indicator with Roman Numerals	
	5.3.6 Possessive Endings	
	5.3.7 Large Roman Numerals	
5.4	Roman Numerals Used as Identifiers	
5.5	Mathematical Letter Combinations Similar to Roman Numerals	Practice
Non-Dec	rimal Bases	
5.6	Letters Used to Represent Numerals in Non-Decimal Bases	
	5.6.1 Transcriber's Note Required	
5.7	Non-Alphabetic Symbols Used to Represent Numerals	Practice
OTHER A	LPHABETS	
5.8	Alphabetic Indicators	
	5.8.1 Code Switching and Use of Letter Indicators	
	5.8.2 Capitalization and Punctuation	
5.9	Greek Alphabet	
	Greek Alphabet Table	
	5.9.1 Code Switching with Greek Letters	
	5.9.2 Alternate Form of Greek Letters	Practice
5.10	German Alphabet	
5.11	Hebrew Alphabet	
5.12	Russian Alphabet	Practice
5.13	A Sequence of Unspaced Letters	
	5.13.1 Derivatives	
5.14	Mathematical Constant	Practice
ENCLOS	ED LISTS	
5.15	Special Case: Definition of "Enclosed List"	
	5.15.1 Nonuse of the Numeric Indicator in an "Enclosed List"	
	5.15.2 Nonuse of the English Letter Indicator in an "Enclosed List"	
	5.15.3 Format: Keep Together	

MORE ABOUT ENGLISH LETTERS

- 5.16 English Letters and Grouping Symbols
- 5.17 English Letters and Endings

MORE ABOUT ABBREVIATIONS

- 5.18 More Spacing Rules
 - 5.18.1 Spacing of Abbreviations With Operation Signs
 - 5.18.2 Spacing of Omission Symbols
- 5.19 Single-Letter Abbreviations
- 5.20 Abbreviations Whose Letters Correspond to a Shortform
- 5.21 Context Clues
- 5.22 Fully Capitalized Acronyms
- 5.23 UEB vs. Nemeth Code

CODE SWITCHING, cont.

5.24 Initiating Nemeth Code Before Itemized Material, Following a Heading5.24.1 Centered Heading5.24.2 Cell-5 and Cell-7 Heading

Answers to Practice Material

Lesson 6

SIGNS OF OPERATION, cont.

6.1	Review of Signs of Operation
6.2	Signs of Operation Using Plus and Minus
6.3	Signs of Operation That Look Like Literary Symbols
	6.3.1-6.3.6 Ampersand; Asterisk; Crosshatch; Dagger and
	Double Dagger; Paragraph Mark; Section
	Mark
6.4	Signs of Operation Unique to Mathematics
	6.4.1-6.4.12 Slash; Back Slash; Dot; Hollow Dot;
	Intersection; Logical Product; Logical
	Sum; Minus With Dot Over; Tilde; Union;
	Vertical Bar; Negated Vertical Bar
Format: Si	imple Tables
6.5	Introduction to Table Format
SIGNS OF	COMPARISON, cont.
6.6	Review of Signs of Comparison
6.7	More Signs of Comparison
	6.7.1–6.7.16 Greater Than With Curved Sides; Less Than With

Downward; Equivalence; Identity (Triple Bar); Inclusion; Membership; Parallel To; Perpendicular To;

Curved Sides; Arc, Concave Upward; Arc, Concave

xiv

Practice 5H

Practice 51

Practice 6A

Practice 6B

		Relation; Reverse Inclusion; Reverse Membership;	
		Tilde as a Sign of Comparison; Variation; Vertical Bar	
	6.7.16.	a Colon Meaning "Such That"	Practice 6C
6.8	Signs of Com	parison Compounded Vertically	
	6.8.1–6.8.9	Greater Than Or Equal To; Inclusion; Intersection;	
		Less Than Or Equal To; Logical Product; Logical Sum;	
		Reverse Inclusion; Tilde; Union	Practice 6D
6.9	Signs of Com	parison Compounded Horizontally	
	6.9.1–6.9.2 (Greater Than; Less Than	
6.10	Negated Sign	s of Comparison	Practice 6E
Format: L	NSTRUCTION	'S	
6.11	Margins for I	nstructions Preceding Itemized Material (5-3)	
	6.11.1 Code	Switching and Instructions	
6.12	Not "Instruct	ions"	
	6.12.1 Margi	ins for Instructions Preceding Unitemized Material (3-1)	
	6.12.2 Itemiz	zed Instructions	
	6.12.3 Margi	ins for Narrative Preceding Itemized Material (3-1)	Practice 6F
Answers to	o Practice Mat	erial	
Lesson	7		
TYPEFOR	2MS		

7.1 Introduction to Typeforms

LETTERS A	AND N	UMERALS
-----------	-------	---------

7.2 Determining Significance of a Variant Typeform

THE FOUR MATHEMATICAL TYPEFORM INDICATORS

- 7.3 Mathematical Typeforms and Their Indicators
- 7.4 Boldface, Italic, Script, and Sanserif Type for Letters and Numerals
- 7.5 Typeform Indicators with One Letter
- 7.5.1 Recognition of Script Type in Other AlphabetsPractice 7A7.5.2 Script Letter of Special Interest
 - 7.5.3 Boldface Letters of Special Interest-Vectors
 - 7.5.4 Boldface Letters of Special Interest—German Letters
- 7.6 Typeform Indicators with One Numeral
 - 7.6.1 Boldface Zero
- 7.7 Nonregular Typeform next to Signs of Grouping
 - 7.7.1 Nonregular Typeform in an Enclosed List
 - 7.7.2 Nonregular Typeform in Contact with a Grouping Symbol Practice 7B

Typeform Indicators with More Than One Letter or Numeral

- 7.8 More Than One Letter
- 7.9 More Than One Numeral

Other Details

7.10	Underlining and Other Typeforms	
7.11	Termination of a UEB Typeform Passage	
	7.11.1 Capitalization	
7.12	Context Clues	Practice 70
BOLDFA	CED MATHEMATICAL SYMBOLS	
7.13	Dots 456	
	7.13.1 Signs of Operation in Boldface Type	
	7.13.2 Equals Sign in Boldface Type	
	7.13.3 Grouping Signs in Boldface Type	Practice 7L
СОМРОЦ	IND EXPRESSIONS	
7.14	Definition of "Compound Expression"	
	7.14.1 Extent of Capitalization	
	7.14.2 Hyphen Followed by a Number	
7.15	Typeform Indicators in Compound Expressions	Practice 7E
Typeform	1 Summary	
UNSPACI	ED NUMBER/LETTER COMBINATIONS	
7.16	Number/Letter Combinations Without Hyphens	
REVISITI	NG THE NUMERIC INDICATOR	
7.17	Summary of the Numeric Indicator	Practice 7F
7.18	Format: Margins for Itemized Material with Subdivisions (1-5; 3-5)	
	7.18.1 Paragraphs Within Itemized Material with Subdivisions (7-5)	
	7.18.2 Side-by-Side Option	Practice 70
	7.18.3 Tabular Form	
	7.18.3.a When to Retain Column Format	
	7.18.3.b When Not to Retain Column Format	

LEVEL IN	IDICATORS	
8.1	Definition	
Superscr	ipts	
8.2	Superscript Level Indicator	
	8.2.1 Abbreviations with Superscripts	Practice 8A
8.3	Returning to the Baseline Level	
8.4	Raised Hollow Dot	Practice 8B
Introduc	tion to the Baseline Indicator	
8.5	Function of the Baseline Indicator	
	8.5.1 Abbreviations with Superscripts	Practice 8C
8.6	Higher Levels of Writing	

	8.6.1 Combinations	
8.7	Certain Raised Signs	
	8.7.1 Raised Ordinal	
	8.7.2 Prime Sign	
	8.7.3 Apostrophe-s	Practice 8D
Subscrip	ts	
8.8	Subscript Level Indicators	Practice 8E
8.9	Returning to the Baseline Level	Practice 8F
8.10	Special Case: Nonuse of the Subscript Level Indicator	
	8.10.1 Further Conditions	
	8.10.2 Restrictions	
	8.10.3 Rewind	
	8.10.4 Summary	Practice 8G
8.11	Spaces Within Superscripts and Subscripts	
	8.11.1 Comma	
	8.11.2 Words	
	8.11.3 Comparison Signs	
	8.11.4 Ellipsis or Long Dash in Superscripts and Subscripts	
	8.11.5 Ellipsis or Long Dash on the Baseline of Writing	
	8.11.6 Segmented Numbers	Practice 8H
More abo	out Superscripts and Subscripts	
8.12	Superscript and Subscript Combinations	Practice 8I
8.13	Left Subscripts and Superscripts	
	8.13.1 Raised Negative Sign	
	8.13.2 More About the Temperature Abbreviations F (Fahrenheit)	
	and C (Centigrade)	
8.14	Further Combinations	
8.15	Consecutive Superscripts and Consecutive Subscripts	
8.16	Simultaneous Superscripts and Subscripts	
8.17	Nonsimultaneous Superscripts and Subscripts	
8.18	Detached Superscripts and Subscripts	
8.19	Literary Symbols and Level Indicators	
Summary	,	Practice 8J
GROUPIN	NG SIGNS, cont.	
8.20	Review of Rules	
8.21	Grouping Symbols and Level Indicators	
8.22	Grouping Symbols with Super/Subscripts	
8.23	More Signs of Grouping	
8.24	Transcriber-Devised Grouping Symbols	Practice 8K
NTRODI	ICTION TO DISPLAYED MATHEMATICAL EXPRESSIONS	
8.25	Displayed Mathematical Expressions	
	8.25.1 Placement of Code Switch Indicators	
	8.25.2 Look for Context Clues	

xvii

8.26 Displayed Narrative Material

Practice 8L

Answers to Practice Material

INTRODU	JCTION TO FRACTIONS	
9.1	Recognition and Layout	
Simple F	ractions	
9.2	Definition of Simple Fraction	
9.3	Simple Fraction Indicators	
	and the Horizontal Simple Fraction Line	Practice 9A
9.4	The Diagonal Simple Fraction Line	
	9.4.1 Use of simple fraction indicators with the diagonal	
	simple fraction line	
	9.4.2 Nonuse of simple fraction indicators with the diagonal simple	
	fraction line	
	9.4.3 Reminder About the UEB Slash	
9.5	Additional Considerations	
	9.5.1 Fractions and Abbreviations	
	9.5.2 Code Switch Reminders	Practice 9B
Mixed N	umbers	
9.6	Definition of Mixed Number	
	9.6.1 Use of Mixed Number Fraction Indicators	
	9.6.2 Mixed Numbers and Omissions	
	9.6.3 Nonuse of Mixed Number Fraction Indicators	Practice 9C
Complex	Fractions	
9.7	Definition of Complex Fraction	
	9.7.1 Use of Complex Fraction Indicators	
	and Complex Fraction Lines	Practice 9D
More Fre	action Rules	
9.8	Fractions and the Baseline Indicator	
9.9	Further Observations Regarding Spacing	
9.10	Fractions and the Ellipsis and Long Dash	
9.11	Enclosed Lists	Practice 9E
RADICAL	EXPRESSIONS	
9.12	Terminology	
9.13	The Termination Indicator	
9.14	Spacing	
9.15	Index of Radical	Practice 9F
9.16	Nested Radical Expressions	
	9.16.1 Nested Radical Expression with an Index	

9.17	Radical Expressions and the Baseline Indicator	
9.18	Radical Expressions and the Ellipsis and Long Dash	
9.19	Radical Expressions and Abbreviations	
9.20	Enclosed Lists with Radical Expressions	Practice 9G
LINKED I	EXPRESSIONS	
9.21	Definition of Linked Expression	
9.22	Division of Linked Expressions	
	9.22.1 Restrictions	
	9.22.2 Other Considerations	Practice 9H
9.23	Special Case: Certain Displayed Linked Expressions	
Format: N	Aargin Requirements for a Linked Expression Requiring	
	Special Margins	
	9.23.1 In Narrative	
	9.23.2 In Itemized Text Without Subdivisions	
	9.23.3 In Itemized Text With Subdivisions	Practice 91

Answers to Practice Material

ARROWS		
10.1	Arrows Used in Mathematics	
Construction	n of Braille Arrows	
10.2	Introduction to the Shape Indicator	
10.3	Horizontal Arrow Shafts	
10.4	Arrowheads	
	10.4.1 Barbed Arrowheads	
10.5	Arrows With Barbed Ends	
10.6	Spacing and Punctuation with Arrows	
10.7	The Contracted Form of the Right-Pointing Arrow	
	10.7.1 Nonuse of the Contracted Form	
	of the Right-Pointing Arrow	Practice 10A
10.8	Arrows With Dotted Ends	
10.9	Arrows With Other Types of Arrowheads	Practice 10B
Vertical, Sla	nted, and Curved Arrow Shafts	
10.10	Arrow Direction Indicators	
	10.10.1 Vertical Arrow Directions	
	10.10.2 Slanted Arrow Directions	
10.11	Curved Arrows	Practice 10C
Boldface and	d Compounded Arrows	
10.12	Boldface Arrows	
10.13	Arrows Used as Signs of Comparison Compounded Vertically	

10.14	Arrows Used as Signs of Comparison	
	Compounded Horizontally	Practice 10D
10.15	Other Arrows	
INTRODUCT	TION TO SPATIAL ARRANGEMENTS	
10.16	Background	
Spatial Arra	ingements with Addition and Subtraction	
10.17	Numeric Indicator	
10.18	Separation Line	
10.19	Alignment with Addition and Subtraction	
10.20	Placement of Symbols	
	10.20.1 Operation Symbols	
	10.20.2 Currency Symbols	
10.21	Side-by-Side Layout	
	10.20.1 Page Number Restriction	
10.22	Blank Lines	Practice 10E
10.23	Omissions in Work Arranged Spatially for Computation	
10.24	Polynomials	
10.25	Abbreviations	
10.26	Fractions	
10.27	Placement of Identifiers	
	10.27.1 Side-by-Side Arrangement	
	10.27.2 Page Number Restriction	Practice 10F
10.28	Carried Numbers with Addition	
10	0.28.1 Placement of Identifiers with Carried Numbers	
Introduction	n to Cancellation	
10.29	Cancellation in Subtraction Problems	
	10.29.1 Placement of Identifiers with Spatial Subtraction	Practice 10G
Arrangemer	nt on the Page	
10.30	Blank Lines and the Page Change Indicator	
10.31	Pagination and Blank Lines	
	10.31.1 Starting a Braille Page with a Spatial Arrangement	
	10.31.2 Ending a Braille Page with a Spatial Arrangement	
10.32	Wide Arrangements	
10.33	Itemized Spatial Problems with Subdivisions	
Placement of	of Code Switch Indicators	
10.34	Opening Nemeth Code Indicator	
10.35	Nemeth Code Terminator	
10.36	Braille Page Turn	
10.37	Instructions Preceding Itemized Spatial Arrangements	
10.38	Displayed Spatial Arrangements	

Answers to Practice Material

SIGNS OF	F SHAPE	
11.1	Definition	
Basic Sh	apes	
11.2	Basic Signs of Shape Represented by Numbers—Regular Polygons	
	11.2.1 Unlisted Regular Polygons	
11.3	Basic Signs of Shape Represented by Letters—Irregular Polygons	
	11.3.1 Unlisted Irregular Polygons	
11.4	Other Basic Signs of Shape Represented by Letters	
	11.4.1 Other Unlisted Basic Shapes	
11.5	Basic Signs of Shape Represented by Other Dot Combinations	
11.6	Filled-In and Shaded Shapes	Practice 11A
Shapes w	vith Structural Modification	
11.7	Definition and Construction	
11.8	Structurally Modified Triangles	
11.9	Structurally Modified Angles	
11.10	Unlisted Shapes with Structural Modification	Practice 11B
Shapes w	vith Interior Modification	
11.11	Definition and Construction	
11.12	Circles with Interior Modification	
11.13	Angles with Interior Modification	
11.14	Rectangles and Squares with Interior Modification	
11.15	Words Enclosed in Shapes	
11.16	Two or More Vertically Arranged Modifiers	
11.17	Two or More Horizontally Arranged Modifiers	
11.18	Unlisted Shapes with Interior Modification	Practice 11C
Other De	etails	
11.19	Spacing with Signs of Shape	
11.20	Punctuation with Signs of Shape	
11.21	Plurals/Possessives	
11.22	Further Considerations Regarding Transcriber-Devised Shapes	
	11.22.1 Usage Rules Regarding Interior Numerals and Arrows	
	11.22.2 Shapes Represented by Drawing	Practice 11D
Calculat	ors and Keyboards	
11.23	The Keystroke Indicator	
	11.23.1 Shape in Print	
11.24	Other Details Concerning Keystrokes	
	11.24.1 The Label	
	11.24.2 Spacing	
11.25	Long Keystroke Constructions	
Icons		
11.26	Consistency in Representation of Icons	

Shapes Used as Signs of Omission

Shupes	sea as signs of omission	
11.27	Spacing	
11.28	The English Letter Indicator and Comparison Signs	
11.29	Use of the Multipurpose Indicator	
11.30	Omissions in Spatially-Arranged Problems	Practice 11E
Identified	d Signs of Shape	
11.31	Spacing	
	11.31.1 Keep Together	
	11.31.2 Surrounding Symbols	
11.32	A Shape Within a Superscript or a Subscript	
11.33	A Shape Which Carries a Superscript or a Subscript	
11.34	The English Letter Indicator	
	11.34.1 The Letter "m"	
11.35	Use of the Numeric Indicator in an Enclosed List	Practice 11F
LABELEL) FORMATS, cont.	
Displaye	d Material with Labels	
11.36	Recognition	
	11.36.1 Braille Layout	
	11.36.2 Transcriber's Note Required	
11.37	Page Number Citation	Practice 11G
TYPEFOR	RMS, cont.	
Labeled	Mathematical Statements	
11.38	Recognition of a Labeled Mathematical Statement	
	11.38.1 The Label	
	11.38.2 The Statement	
	11.38.3 Spacing and Margins	
11.39	Significant Typeface	Practice 11H
Typeform	n Indicators for Mathematical Words and Phrases	
11.40	Italic and Boldface Typeform Indicators	
	11.40.1 One Word in Italics or Boldface	
	11.40.2 A Phrase in Italics or Boldface	
11.41	Code Switching Within an Emphasized Passage	
11.42	Revisiting Typeform in Labeled Statements	Practice 111
Answers to	o Practice Material	

Lesson 12

MODIFIERS AND MODIFIED EXPRESSIONS

12.1 Definition

12.2 Construction of Simple Modified Expressions – The Five-Step Rule

Common Modifiers

12.3 Arrows as Modifiers

	Special Situations Involving Arrows	
	12.3.1 When to Omit Arrows	
	12.3.2 When the Arrow is Being Modified	
	12.3.3 When Other Rules Apply	Practice 12A
12.4	Carets as Modifiers	
12.5	Horizontal Bar as a Modifier	
	12.5.1 The Contracted Form of Bar Over/Bar Under	
	12.5.1.a Bar Above	
	12.5.1.b Bar Below	Practice 12B
12.6	Other Symbols as Modifiers	
	12.6.1 Dot	
	12.6.2 Arc	
	12.6.3 Tilde	
	12.6.4 Question Mark	
12.7	Expressions as Modifiers	
	12.7.1 Binomial Coefficient	Practice 12C
12.8	Spacing with Modified Expressions	Practice 12D
Modified	l Expressions and Superscripts/Subscripts	
12.9	Modified Expression on the Baseline	
	12.9.1 Superscript/Subscript After the Modification	
	12.9.2 Superscript/Subscript Within the Modification	
	12.9.3 Binomial Coefficient	Practice 12E
	12.9.4 Modified Expression on the Baseline That Follows a	
	Superscript or a Subscript	
12.10	Modified Expression Within a Superscript or Subscript	Practice 12F
12.11	Horizontal Grouping Signs as Modifiers	
Modified	l Signs of Comparison	
12.12	Definition	
12.13	Transcription	Practice 12G
Expressi	ons with More Than One Modifier	
12.14	Modifiers of Higher Order	
	12.14.1 Parallel Horizontal Bars	
12.15	Individual Modifiers	
12.16	Simultaneous Modifiers	Practice 12H
Format: F	FORMAL PROOF	
12.17	Definition	
	12.17.1 Spacing and Margins	
	12.17.2 Auxiliary Captions	
	12.17.3 Step-Number Format	Practice 12I
		Practice 12J
SPATIAL	ARRANGEMENT WITH MULTIPLICATION	
12.18	Alignment	
12.19	Placement of Multiplication Symbol	

xxiii

12.20 Separation Line

Alignment of Partial Products

12.21	Partial Products	
	12.21.1 Spacing	Practice 12K
12.22	Omissions	
12.23	Fractions and Mixed Numbers	
12.24	Polynomials	
12.25	Subscripts Denoting Nondecimal Bases	
12.26	Carried Numbers with Multiplication	
12.27	Placement of Identifiers with Spatial Multiplication	Practice 12L
Answers t	o Practice Material	

	xxiv	
	13.4.3 Punctuation	Practice 13C
	13.4.2 Spacing	
	13.4.1 Grouping	
13.4	Tally Mark	
	13.3.1 Punctuation	
13.3	Angstrom Unit	
Spacing	with the Angstrom Unit and Tally Marks	
	13.2.6 Boldface Vertical Bar (end of proof)	Practice 13B
	13.2.5 Therefore	
	13.2.4 Since (because)	
	13.2.3 Ditto Marks	
	13.2.2 Check Mark	
	13.2.1 "At" Sign in Mathematical Context	
13.2	Spacing Rules for Spaced Symbols	
Spaced N	Tiscellaneous Symbols	- , werree 1 5/1
	13.1.9 Ouantifiers	Practice 13A
	13.1.8.a Upper and Lower Integral Signs	
	13.1.8 Integral	
	13.1.7 Infinity	
	13.1.6 Factorial Sign	
	13.1.5 Empty Set (null set void set)	
	13.1.5 Der	
	13.1.2 Crossed Letters	
	13.1.1.a Use of the UEB Caret	
	13.1.1 Caret	
13.1	Spacing Rules for Unspaced Symbols	
Unspace	d Miscellaneous Symbols	
MISCELL	ANEOUS SYMBOLS	
MOODIT		

SUPERPOSED SIGNS

13.5	Definition and Analysis		
13.6	Transcription of Superposed Signs		
	13.6.1 Integral Modified by Superposition		
	13.6.2 Signs of Operation Modified by Superposition		
	13.6.3 Horizontal and Vertical Bars Modified by Superposition		
	13.6.4 Signs of Shape Modified by Superposition		
	13.6.5 Signs of Comparison Modified by Superposition		
	13.6.6 Symbols That Are Not Superposed Signs	Practice 13D	
AMBIGU	OUS SIGNS		
13.7	Context		
	13.7.1 Vertical Bar and Colon		
	13.7.2 Spacing		
	13.7.3 Uppercase Greek Letters		
	13.7.4 Chemical Notation	Practice 13E	
MULTIPU	JRPOSE INDICATOR		
13.8	Review		
13.9	Additional Uses of the Multipurpose Indicator		
	13.9.1 Letter Followed by a Decimal Point and a Numeral		
	13.9.2 Numeric Subscript Followed by a Numeral		
	13.9.3 Decimal Point Followed by a Nonnumeric Character		
	13.9.4 Side-by-Side Vertical Bars	Practice 13F	
DIVISION	PROBLEMS		
13.10	Linear Representation	Practice 13G	
SPATIAL	ARRANGEMENTS WITH DIVISION		
13.11	Notation Devices		
	13.11.1 Length of the Separation Line		
13.12	When a Spatial Arrangement is Required		
	13.12.1 More Than Just Numerals		
	13.12.1.a Spacing with Abbreviations		
	13.12.2 A Quotient is Present		
	13.12.2.a A Quotient with a Remainder		
	13.12.3 Long Division	Practice 13H	
13.13	Blank Lines Required		
13.14	Omissions		
13.15	Carried Numbers in Long Division		
13.16	Cancellation in Long Division		
13.17	Placement of Identifiers with Spatial Division	Practice 131	

Answers to Practice Material

FUNCTIC	ON NAMES AND THEIR ABBREVIATIONS	
14.1	Functions	
	14.1.1 Code Switching	
14.2	Spacing of Function Names	
	14.2.1 Spacing with Signs of Operation	
	14.2.2 Spacing with Indicators	Practice 14A
14.3	Nonuse of the English Letter Indicator	
14.4	Unabbreviated Function Names in Mathematical Context	
14.5	Consecutive Function Names	
	14.5.1 "Arc" in Context	
	14.5.1.a Do Not Confuse	
14.6	Punctuation	
14.7	Keep Together	
14.8	Clarification—Function Names in an Enclosed List	Practice 14B
14.9	Function Names and Superscripts/Subscripts	
	14.9.1 Use/Nonuse of the Subscript Indicator	
	14.9.2 Function Names Within a Superscript or a Subscript	Practice 14C
14.10	Modifiers with Function Names	
	14.10.1 Special Case: Upper Limit and Lower Limit	Practice 14D
Format: L	Division of Mathematical Expressions Between Braille Lines	
14.11	Review	
14.12	The Concept of Logical Mathematical Units	
	14.12.1 The Priority List	
14.13	Priority #1—Before a Sign of Comparison	
	14.13.1 Identifier May Stand Alone	
	14.13.2 Logical Mathematical Units	
14.14	Priority #2—Before a Sign of Operation	
	14.14.1 Logical Mathematical Units	Practice 14E
14.15	Priority #3—Before a Fraction Line	
	14.15.1 Logical Mathematical Units	
14.16	Priority #4—Before a Baseline Indicator	
	14.16.1 Logical Mathematical Units	Practice 14F
14.17	Priority #5—Before a Level Indicator	
14.18	Priority #6—Between Grouped Factors	
	14.18.1 Logical Mathematical Units	
14.19	Priority #7—After a Termination Indicator	Practice 14G
14.20	Application of this Rule to Special Linked Expressions	
	14.20.1 Long Anchor	
	14.20.2 Long Link	Practice 14H
14.21	Margins for Embedded Expressions	
14.22	Items That Must Not Be Divided	

14.22.1	Symbol	ls to Keep	Together
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14.22.2 Expressions to Keep Together

Spatial Arrangements, cont.

SQUARE ROOT DIVISION

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14.23	Review of Terminology	
14.24	Spatial Arrangement for Square Root Problems	
14.25	Placement of Identifiers with Spatial Radical Expressions	Practice 14I
OTHER P	RINT LAYOUTS SHOWING DIVISION	
14.26	Partial Quotients	
14.27	Synthetic Division	
	14.27.1 Alignment and Spacing	
	14.27.2 Vertical Line	
	14.27.3 Another Print Style—Divisor on the Right	
	14.27.4 Another Print Style—Boxed Divisor	
	14.27.5 Placement of Identifiers with Synthetic Division	Practice 14J
Answers to	o Practice Material	

SPATIAL	ARRANGEMENTS OF FRACTIONS			
15.1	Spatial Fraction Line			
15.2	Numerator and Denominator			
15.3	Placement of Identifiers with Spatially Arranged Fractions			
Situation	s Requiring Spatial Presentation			
15.4	Simple Fractions Arranged Spatially for Illustration	Practice 15A		
15.5	Cancellation Within Fractions			
	15.5.1 Extent of Cancellation			
	15.5.2 Cancellation and Level Indicators			
	15.5.3 Canceled Abbreviations			
15.6	Chemistry Exception	Practice 15B		
HYPERCO	OMPLEX FRACTIONS			
15.7	Definition and Recognition			
15.8	Hypercomplex Fraction Indicators			
15.9	Higher Orders of Complexity	Practice 15C		
CONTINUED FRACTIONS				
15.10	Definition and Recognition	Practice 15D		
Format: R	EMARKS AND COMMENTS			
15.11	Guidelines			
	15.11.1 OPTION #1-Continue the Commentary on the Same Line			
	15.11.2 OPTION #2—Indent the Commentary on the Next Line	Practice 15E		
Format: STEM-AND-LEAF PLOTS				
15.12	Definition and Recognition			

- 15.14 The Key
- 15.15 Data Consisting of More Than One Character; Punctuation Between Entries

Practice 15F

- 15.16 Alphabetic Data
 - 15.16.1 Alphabetic Key
- 15.17 Blank Entries
- 15.18 Runovers Within the Table
- 15.19 Back-To-Back Plot

Answers to Practice Material

SYSTEMS OF	FEQUATIONS				
16.1	Definition and Recognition				
16.2	Transcription Rules for Systems of Equations	Practice 16A			
16.3	Unified System of Equations and Enlarged Grouping Signs				
Enlarged Sig	gns of Grouping				
16.4	Transcription Rules for Enlarged Signs of Grouping				
	16.4.1 Enlarged Left Brace				
	16.4.2 Enlarged Right Brace				
16.5	Embedded Vertical Groupings	Practice 16B			
16.6	16.6 Enlarged Parentheses				
16.7	Placement of Symbols				
16.8	Placement of Identifiers and Punctuation				
16.9	Grouping Symbols Shown Taller in Print	Practice 16C			
16.10	Remarks Printed Next to Spatial Arrangements				
	16.10.1 Remarks Brailled Beside Unified Expressions				
	16.10.2 Remarks Brailled Below the Arrangement	Practice 16D			
16.11	More Enlarged Signs of Grouping	Practice 16E			
DETERMINA	INTS AND MATRICES				
16.12	Definition and Recognition				
16.13	Transcription Rules for Determinants and Matrices				
	16.13.1 Blank Lines				
	16.13.2 Grouping Symbols				
	16.13.3 Placement of Items				
	16.13.4 Numeric and Letter Indicators				
	16.13.5 Placement of Identifiers, Symbols, and Punctuation	Practice 16F			
Further Con	nsiderations with Determinants and Matrices				
16.14	Multiplying Arrays				
16.15	Omission Dots				
	16.15.1 No Dots Are Printed Between Columns				
	16.15.2 Dots Are Printed Between Columns or				
	Some Entries are Blank	Practice 16G			

16.16	Space-S	Saving T	Techniques
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16.16.1 Runovers With Indentation

- 16.16.2 Runovers Without Indentation
- 16.16.3 Fractions in Arrays

16.16.4 Keying

16.17 Row Matrix

16.18 Embedded Arrays

16.19 Use of Tactile Graphics for Enlarged or Horizontal Grouping Signs

Answers to Practice Material

Lesson 17

TABLES 17.1 Structure of Tables 17.2 Table Label and Title 17.3 Column Headings 17.4 Table Entries 17.4.1 Tables in UEB 17.4.2 Tables in Nemeth Code 17.4.3 Code Switching Decisions Practice 17A 17.5 When Row Headings are Words Practice 17B Boxed Tables 17.6 Code Switching and Box Lines 17.6.1 Switching Within the Table 17.6.2 Switching Within the Box Lines 17.6.3 Technical Material Before or After a Box 17.6.4 Placement of Transcriber's Note Practice 17C Table Rules Specific to the Nemeth Code 17.7 Table of Numbers Practice 17D FIGURES AND DIAGRAMS 17.8 Which Code? 17.8.1 Letters Used as Diagram Labels 17.9 Switch Indicators and Tactile Graphics 17.10 Graphic Number Lines Practice 17E 17.11 Diagrams in Exercise Material KEYING TECHNIQUE 17.12 Keying 17.12.1 Alphabetic Key 17.12.2 Numeric Key 17.12.3 The Key List Practice 17F

Practice 16H

Practice 16I

CHEMISTRY

17.13 Two BANA Publications

Answers to Practice Material

Lesson 18

- 18.1 Preparing for the Certification Exam
- 18.2 The Nemeth Codebook
- 18.3 Beyond the Nemeth Code

Structuring a Textbook

- 18.4 Transcriber-Generated Pages and Front Matter
 - 18.4.1 Special Symbols Page
 - 18.4.1.a Braille Order
 - 18.4.2 Transcriber's Notes Page
- 18.5 Body of Text
 - 18.5.1 Follow Nemeth Code Formatting Rules
 - 18.5.2 Follow Braille Formats Formatting Guidelines
 - 18.5.3 Context-Dependent Formats

Four Practices

Practice 18B Practice 18C Practice 18D Practice 18E

Practice 18A

Answers to Practice Material

Appendices

- Appendix A Reading Practice
- Appendix B Glossary Of Terms

Appendix C Nemeth Code Format Summaries

Appendix D Sample Page